

ACCURATE TOP OF THE ATMOSPHERE ALBEDO DETERMINATION FROM MULTIPLE VIEWS OF THE MISR INSTRUMENT

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Introduction

Multi-angle Imaging Spectro-Radiometer (MISR):

- EOS-AM platform, launch in 1998
- Nine cameras - zenith angles of $\pm 70.5^\circ$, $\pm 60^\circ$, $\pm 45^\circ$, $\pm 26.1^\circ$ and 0 degrees in the along track direction
- Four spectral channels: 443 nm (blue), 550 nm (green), 670 nm (red) and 865 nm (near infrared)
- Misc: 275m pixels, 360 km swath, 9 day repeat
- Global Data Products: (geo-referenced)
 - Top of the atmosphere spectral albedo (2.1km and 31km) (clear and cloudy conditions)
 - Surface hemispherical-directional reflectance factor (ocean: 2.1km and land: 1.1km),
 - Aerosol distributions (ocean: 2.2km and land: 17.6km).

Definition of TOA Albedo

The albedo in each MISR channel c , $c = [1, 2, 3, 4]$ is defined according to Nicodemus et al, 1977, as:

$$\alpha_{0c}(\mu_s) = \frac{1}{\pi} \int_0^{\pi} \int_0^{2\pi} d\phi_s d\phi_v BRF_c(\mu_s, \mu_v, \phi_s), \quad (1)$$

with the notation:

$\alpha_{0c}(\mu_s)$ is the top of atmosphere albedo in MISR channel c ,

ϕ_s is the angle relative to the solar azimuth,

μ_s is the cosine of the solar zenith angle θ_0 ,

μ_v is the cosine of the view zenith angle θ_v and

$BRF_c(\mu_s, \mu_v, \phi_s)$ is the bidirectional reflectance factor in MISR channel c .

Relationship between the BRF and the bidirectional reflectance distribution function BRDF is:

$$BRDF_c(\mu_s, \mu_v, \phi_s) = \frac{1}{\pi} BRF_c(\mu_s, \mu_v, \phi_s). \quad (2)$$

The BRF_c is related to the radiance I_c by the following equation:

$$BRF_c(\mu_s, \mu_v, \phi_s) = \frac{\pi I_c(\mu_s, \mu_v, \phi_s) D^2}{\mu_s E_{0c}} \quad (3)$$

where $D = R(t)/R_0$ is the normalized distance to the sun, $R(t)$ is the time dependent distance and R_0 is the distance for which E_{0c} is defined and E_{0c} is the TOA solar irradiance.

Simulated MISR Data Set

Motivation:

- No MISR data yet available
- Clear sky TOA albedo algorithm must be available at launch

Requirements for simulated data set:

- "Radiative transfer" (RT) code must include BRDF
- Must calculate the multiple scattering for a large range of sun and view angles
- Radiance with an error less than 1% requires an eight stream approximation (two stream approximations can cause up to 20% error)

Two available codes: 6S (Vermote et al, 1994) and JMRT (Mantonchik, 1994). (MODTRAN5 was not available prior to this work)

"John Mantonchik Radiative Transfer" (JMRT) Code

Features:

- Five different aerosol types (urban, rural, maritime, desert and arctic)
- 46 surface BRDF's from experimental data and models:

- vegetation (23),
- bare soil (3),
- rough water surface (11),
- snow and ice (9).

- Computes BRF in 10 zenith and 12 azimuthal angles
- Any additional surface BRDF's can be added
- Number of streams is variable

Albedo calculation:

- Simulated MISR data set uses 1-step Newton-Cotes integration:

$$\alpha_{0c}(\mu_s) = Const \frac{2\pi}{N_\theta - 1} \sum_{i=1}^{N_\theta - 1} \mu_i \sum_{j=1}^{N_\phi - 1} \frac{\mu_j BRF_c(\mu_s, \phi_j) + \mu_{j+1} BRF_c(\mu_s, \phi_j)}{2(\mu_{j+1} - \mu_j)}, \quad (4)$$

where $N_\theta = 12$ is the number of azimuthal and $N_\phi = 10$ is the number of elevation angles, $Const$ is determined by setting $\alpha_{0c}(\mu_s) = 1$ with $BRF_c(\mu_s, \phi_s) = 1$ in eq.(4).

- Inverted BRF model uses numerical integration with iterated Gaussian quadrature over μ_v and ϕ_s

Azimuthal Models for the TOA BRF

Purpose and Requirements :

- MISR measures only in nine discrete directions \Rightarrow estimate the TOA radiance in directions which are not seen by MISR
- Azimuthal model (AZM) described BRF in other directions \Rightarrow semi-empirical function
 - As few parameters as possible,
 - Uniquely invertible
 - Reciprocal (sun and view angles are interchangeable without changing the value)
 - Little sensitivity to noise.

Coupled Surface-Atmosphere Reflectance (CSAR)

$$BRF_{CSAR}(\theta_s, \phi_s, \theta_v, \phi_v) = \frac{\mu_s^{c_s-1} \mu_v^{c_v-1}}{(\mu_s + \mu_v)^{c_s}} F(g) [1 + R(G)], \quad (5)$$

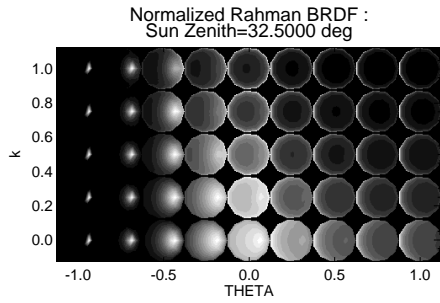
where ϕ_0 and κ are empirical surface parameters between 0 and 1 with the condition on ϕ_0 that the albedo of eq.(5) is between 0 and 1, and $F(g)$ is the Henyey-Greenstein function:

$$F(g) = \frac{1 - \phi_0^2}{[1 + \phi_0^2 - 2\phi_0 \cos(\pi - g)]^2}$$

ϕ_0 controls the forward ($0 \leq \phi_0 \leq 1$) and backward (hot spot) ($-1 \leq \phi_0 \leq 0$) scattering peak, g is a phase angle and given by: $\cos g = \mu_s \mu_v + \sin \theta_s \sin \theta_v \cos(\phi_s - \phi_v)$, $(1 + R(G))$ approximates the hot-spot with:

$$1 + R(G) = 1 + \frac{1 - \phi_0}{1 + G},$$

where $G = \sqrt{\tan^2 \theta_s + \tan^2 \theta_v - 2 \tan \theta_s \tan \theta_v \cos(\phi_s - \phi_v)}$.



Polar representation of the CSAR BRF for $\theta_s = 32.5^\circ$ and $\theta_0 = 0.2$ as a function of ϕ_0 and κ .

Uniqueness

Problem:

Given a BRF slice for a given CSAR parameter set (ϕ_0 , κ and ϕ_{0s}) can we recover the original parameter set using non-linear least square fitting?

Procedure:

- Generate N_θ randomly chosen parameters: ϕ_{0is} , κ and ϕ_{0vi} , $i = 1, 2, 3, \dots, N_\theta$.
- Calculate N_θ BRF slices $BRF(\theta_s, \phi_s, \theta_v, \phi_v; \phi_{0is}, \kappa, \phi_{0vi})$ using eq.(5).
- Invert BRF model for ϕ_{0is} , κ and ϕ_{0vi} .
- Compute errors $\epsilon(\phi_{0i}) = \phi_{0i} - \phi_{0is}$, $\epsilon(\kappa) = \kappa - \kappa$ and $\epsilon(\phi_{0vi}) = \phi_{0vi} - \phi_{0vi}$ and the "Root Mean Square Error" (RMSE) of the BRF slice difference ($BRF_i - BRF_i$).

Result: Yes, the CSAR model appears unique

Noise Sensitivity

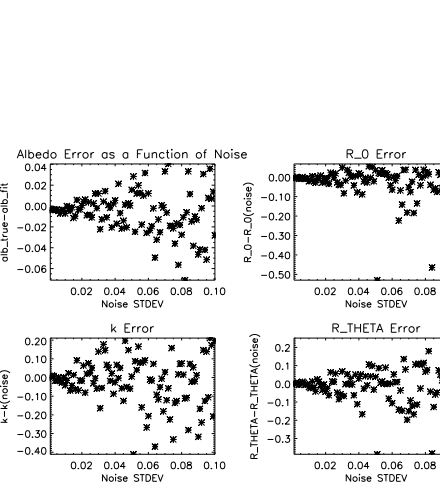
Problems:

(A) How much noise can be tolerated in the inversion? (B) How does the albedo error change as a function of added noise?

Procedure:

- Generate a BRF slice BRF_i for a fixed set of parameters: $\theta_s = 30^\circ$, $\phi_0 = 0.5$, $\kappa = 0.3$ and $\phi_{0s} = 0.22$ and compute the albedo α_0 using a numerical integration technique (e.g. 1-step or 5-step Newton-Cotes integration).
- For $i = 1, \dots, N_\theta$ cases do:
 - $BRF_i = BRF + \sigma_i N(0, 1)$, where $N(0, \sigma_i)$ denotes the i -th realization of a Gaussian distributed random vector with mean 0 and standard deviation σ_i where $\sigma_i = \{1, 2, 3, \dots, N_\theta\} \Delta_\sigma$ and Δ_σ is an increment.
 - Retrieve the BRF parameters: ϕ_{0is} , κ and ϕ_{0vi} and the fitted BRF_i . Compute the albedo α_{0i} of the inverted BRF.
- Plot the BRF_i , BRF_i and BRF_i as a function of MISR camera angle.
- Plot σ_i on the x-axis and $[(\alpha_0 - \alpha_{0i}), (BRF - BRF_i), (\phi_0 - \phi_{0i}), (\kappa - \kappa), (\phi_{0s} - \phi_{0is})]$ on the y-axis.

Results: (A) The error between original and retrieved BRF parameters grows linearly with increased noise. (B) The albedo error was less than $\pm 5\%$ for $\sigma \leq 0.1$ for an albedo of 0.43.



Clear Sky Top of Atmosphere Albedo Algorithm

- Read TOA BRFs from JMRT output.
- For all N_θ cases $k = 1, 2, 3, \dots, N_\theta$ do:
 - Compute the albedo α_{0k} using Newton-Cotes integration over the quadrature angles.
 - For view azimuthal angles $\phi_v = [0^\circ, 30^\circ, 60^\circ, 90^\circ]$ do:
 - Extract a BRF slice (BRF_{ik} , $i = 1, 2, \dots, 9$) at the MISR angles for $(\phi_s, \phi_v + 180^\circ)$.
 - Perform nonlinear curve fit of BRF_{ik} results in estimated CSAR parameters ϕ_{0ik} , κ_{ik} and ϕ_{0vi} .
 - Do a numerical integration of CSAR model over the hemisphere results in estimated albedo α_{0ik} .
 - Compute albedo error: $\epsilon(\alpha_{0ik}) = \alpha_{0k} - \alpha_{0ik}$.
 - Plot standard deviation σ of the albedo error $\epsilon(\alpha_{0ik})$.
 - Generate TOA BRF from estimated CSAR parameters and display.
- Generate scatter plots of standard deviation of the albedo error versus azimuth marking different surface types with symbols.

Results

Error Metric:

Standard deviation σ of the albedo error

Cases:

- 5 different atmospheres
- 3 sun angles (15° , 32.5° , 50°)
- 4 different azimuthal angles (at 0° , 30° , 60° and 90°)

\Rightarrow 2760 cases

Computing time: ≈ 1 h on Sparc 10 (includes visualization)

Note: Faster inversion routines must be found to make this approach practicable for the EOS data information system

Three Parameters (no Limits) CSAR Model

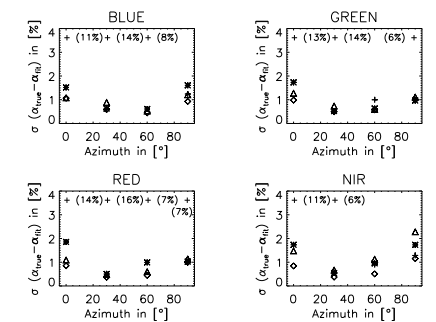
Motivation: Easy to perform nonlinear least squares curve fit without bounded parameters

$$BRF_i(\theta_s, \phi_s) = BRF_{CSAR}(\theta_s, \phi_s; \phi_{0s}, \kappa, \phi_{0v}), i = 1, \dots, 9 \quad (6)$$

Result: For snow and ice which have larger reflectances and a more Lambertian character, the errors exceeded the 5% level for many azimuthal angles.

Reason: The inversion routine which was not able to find a good solution in the 20 iteration limit and RMSE error limits of 0.01.

Note: plot data points outside the 4% limit as symbols with an error in % in brackets.



Symbols used: Δ Vegetation (23 models), \circ Soil and sand (3 models), $+$ Snow and ice (8 models) and $*$ Water (11 models).

Two Parameters (with Limits) CSAR Model

Motivation: MISR does not measure in the principle plane \Rightarrow do not use parameter which models forward or backward scattering

$$BRF_2(\theta_s, \phi_s) = BRF_{CSAR}(\theta_s, \phi_s; \phi_{0s}^*, \kappa^*, F(g) = 1), i = 1, \dots, 9. \quad (7)$$

Variable transform: from the original unbound variable ϕ_0 to the interval limited variable ϕ_0^* was used:

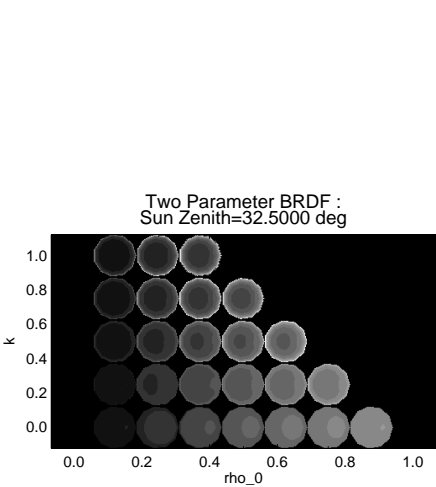
$$\phi_0^* = \frac{1}{2} + \frac{\tan^{-1}(\phi_0)}{\pi}$$

and it's inverse:

$$\phi_0 = \tan(\pi(\phi_0^* - \frac{1}{2})).$$

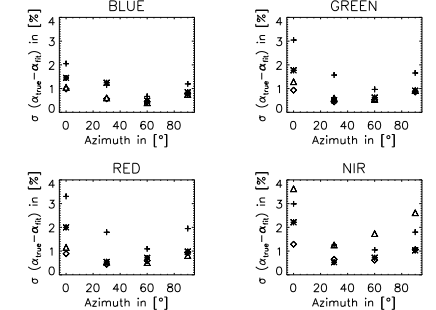
Similarly κ can be transformed to κ^* .

Result: The method works well for all cases and channels ($\sigma < 3.8\%$) For more typical MISR azimuthal angles between 30° and 60° the albedo errors are below 2% which is very good.



Polar representation of the two parameter CSAR BRF for $\theta_s = 32.5^\circ$ as a function of ϕ_0 and κ .

Symbols used: Δ Vegetation (23 models), \circ Soil and sand (3 models), $+$ Snow and ice (8 models) and $*$ Water (11 models).



Atmospheric Transmission Correction

Motivation: Visualizing the resulting TOA BRF fields for the BRF_1 and BRF_2 models we noticed that the BRF near the horizon ($90^\circ < \theta_0 < 90^\circ$) often was very much larger than the computed BRF from JMRT.

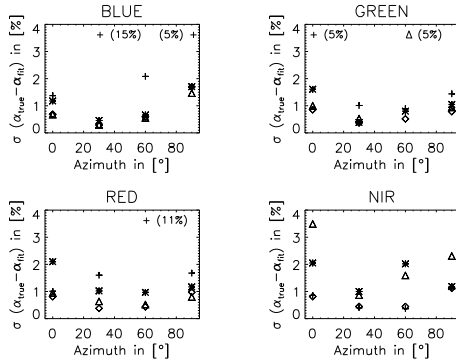
Idea: Include atmospheric terms, e.g. transmission.

$$BRF_3(\theta_i, \phi_i) = BRF_{CSAR}(\theta_i, \phi_i; \theta_0, \kappa; \Theta) \exp(-\tau_c/\mu_i), \quad i = 1, \dots, 9; \quad c = 1, 2, 3, 4 \quad (8)$$

where the mean transmission factor $T_c = \exp(-\tau_c/\mu_i)$ and $\tau_c = [241, -0.04, -0.03, -0.15]$ and c is the channel indicator.

Result: Works well for blue channel and in the principle plane $\phi = 0^\circ$. Converges for all cases for the NIR to less than 3.6% σ .

Symbols used: Δ Vegetation (23 models), \diamond Soil and sand (3 models), $+$ Snow and ice (9 models) and \times Water (11 models).



Atmospheric Pre-Correction

Motivation: Visualizing the resulting TOA BRF fields for the BRF_1 and BRF_2 models we noticed that the BRF near the horizon ($90^\circ < \theta_0 < 90^\circ$) often was very much larger than the computed BRF from JMRT.

Idea: Include atmospheric terms, e.g. transmission and path radiance from Rayleigh scattering.

$$BRF_4(\theta_i, \phi_i) = BRF_{CSAR}(\theta_i, \phi_i; \theta_0, \kappa; \Theta_0) \exp(-\tau_c/\mu_i) - BRF_{Rayleigh}(\theta_i, \phi_i), \quad i = 1, 2, 3, \dots, 9; \quad c = 1, 2, 3, 4 \quad (9)$$

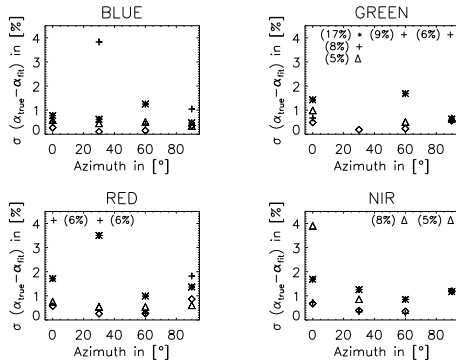
and the albedo is given by the sum of:

$$\alpha_0 = Albedo(BRF_{CSAR}(\theta_i, \phi_j) \exp(-\tau_c/\mu_i)) + Albedo(BRF_{Rayleigh}(\theta_i, \phi_j)), \quad i = 1, 2, 3, \dots, N_0; \quad j = 1, 2, 3, \dots, N_0; \quad c = 1, 2, 3, 4 \quad (10)$$

where $BRF_{CSAR}(\theta_i, \phi_j)$ is the hemispherical BRF computed from the best fit of the CSAR parameters to the BRF slice $BRF_4(\theta_i, \phi_i)$.

Result: Works well for blue channel and in the principle plane $\phi = 0^\circ$. Convergence problems, probably because no limits on the CSAR parameters is used.

Symbols used: Δ Vegetation (23 models), \diamond Soil and sand (3 models), $+$ Snow and ice (9 models) and \times Water (11 models).



Conclusions

- Albedo error is less than 1% in the visible and less than 1.5% in the NIR (only nadir measurements are used the albedo error is about 5% in the visible and 10% in the NIR).
- More work needed to make this approach robustly work for all surfaces and atmospheric conditions.
- Need to perform the inversion more rapidly and flag pixels for which the model did not fit very well.
- This approach lends itself to calculate the hemispherical BRF field over any region of the Earth.

Future Work

- Investigate other semi-empirical BRF models.
- How the BRF-CSAR parameters vary as a function of sun angle?
- Is there a diurnal smooth trajectory for a parameter with sun angle? If so, we could use this to predict the TOA clear sky albedo at times of the day.

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